

**Physics of Aquatic Systems**

**1. Introduction (Properties of Water)**

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**MVEnv3**

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**Physics of Aquatic Systems**

One of four main lectures in Environmental Physics:  
Atmosphere, climate, terrestrial and aquatic systems

Main focus: Lakes, groundwater, isotope hydrology

This lecture builds on fundamental environmental physics (e.g., fluid dynamics) of the lecture MKEP4

For details, updates and lecture notes see  
<http://www.iup.uni-heidelberg.de/institut/studium/lehre/AquaPhys/MVEnv3.html>

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**Overall Contents I**

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**Part I: Aquatic Physics**

1. Introduction (role and physical properties of water)
2. Density stratification and flow in lakes and oceans
3. Turbulent flow in surface waters
4. Ocean circulation
5. Turbulent transport in surface waters
6. Heat and gas exchange
7. Flow and transport in groundwater

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**Overall Contents II**

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**Part II: Isotope Hydrology**

1. Introduction to Isotope Hydrology
2. Stable Isotopes I
3. Stable Isotopes II
4. Tritium and <sup>3</sup>He
5. Dating of Young Groundwater and Modeling
6. Dating of old Groundwater
7. Noble Gases and Paleoclimate

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**Contents of Session 1: Introduction**

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- Definition of "Physics of Aquatic Systems"
  - Compartments of the hydrosphere
- 1.1 The global hydrological cycle
  - Water problems as a motivation for water research
- 1.2 The role of water in the environment
- Physical properties of water
  - 1.3 Specific and latent heat, vapour pressure

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**What is "Physics of Aquatic Systems"?**

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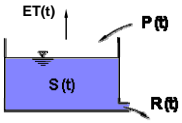
- Study of physical conditions and processes (e.g. stratification, flow, transport, mixing, heat/gas exchange) in natural systems containing liquid water (e.g. lakes, ocean, groundwater)
- Related Disciplines, Subdisciplines:
  - Physical Oceanography and Limnology
  - Hydro(geo)logy and soil physics
  - Meteorology and (paleo)climatology

For comparison: What is **Hydrology**?

- Study of the global water (hydrological) cycle, especially water on the **continents**, above, on, and below the surface
- Classical hydrological systems: Catchments of rivers/aquifers
- Physical aspects: Water balance, water fluxes
- Chemical, biological, and technical/sociological aspects
- Engineering aspects: water supply, flood protection, etc.

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## Hydrologic Water Balance



Hydrological system: reservoir with

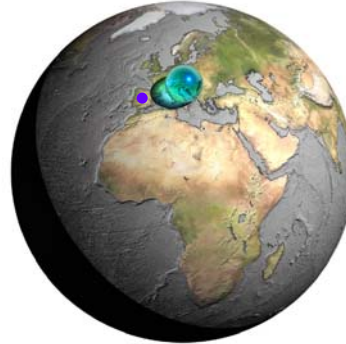
- input P (precipitation)
- output R (runoff)
- output ET (evapotranspiration)

Continuity/Mass conservation: Input – Output = Change in storage

$$P - R - ET = \frac{dS}{dt}$$

- Simple equation, but ...
- ... individual terms are difficult to quantify
- Isotopes may help → Part 2 of this lecture

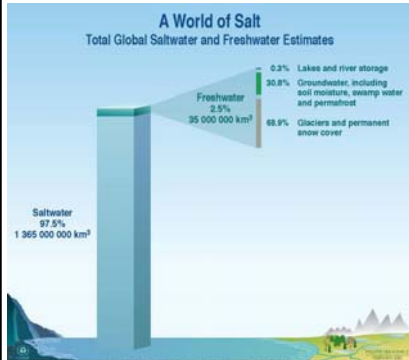
## Water on Earth



All water on Earth:  
 $1.37 \cdot 10^9 \text{ km}^3$   
 Sphere with  $R \approx 700 \text{ km}$   
 thereof 3 % fresh water:  
 $\sim 40 \cdot 10^6 \text{ km}^3$   
 Sphere with  $R \approx 200 \text{ km}$

<http://www.adamnieman.co.uk/vos/index.html>

## Saltwater and Freshwater



Water in env. compartments (blue: Hydrosphere) volumes in  $10^3 \text{ km}^3$

Saltwater: 1'365'000  
 thereof  
 Oceans: 1'365'000  
 Salt lakes (Casp. Sea): 80

Freshwater: 35'000  
 thereof  
 Ice: 24'000  
 Groundwater: 10'800  
 Soil water: 70  
 Lakes: 110  
 (Lake Baikal 23)  
 Atmosphere: 16  
 Rivers: 2  
 Biosphere: 2

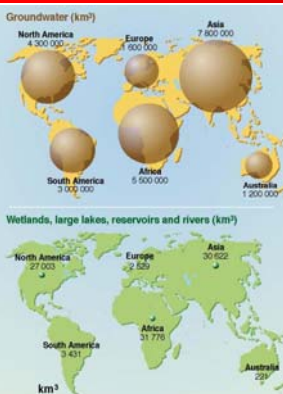
Source: Igor A. Shiklomanov, State Hydrological Institute (SHI, St. Petersburg) and United Nations Educational, Scientific and Cultural Organisation (UNESCO Paris, 1998)  
<http://www.unep.org/vitalwater/index.htm>

## Compartments of the Hydrosphere

	Volume in $10^3 \text{ km}^3$	% of total freshwater	flux $10^3 \text{ km}^3/\text{year}$	turn-over time year
<b>Salt water</b>				
Oceans	1 350 000		425	3000 <sup>1)</sup>
<b>Freshwater</b>				
Ice	27 800	69.3	2.4	12 000 <sup>2)</sup>
Groundwater	8 000 <sup>3)</sup>	29.9	15	500 <sup>3)</sup>
Lakes	220 <sup>4)</sup>	0.55		
Soil moisture	70	0.18	90	0.8 <sup>5)</sup>
Atmosphere	15.5	0.038	496	0.03 <sup>6)</sup>
Reservoirs	5	0.013		
Rivers	2	0.005	40	0.05 <sup>7)</sup>
Biomass	2	0.005		
<b>Total</b>	<b>40 114</b>	<b>100</b>		

from Mook, 2001

## Groundwater and Surface Water



Groundwater:

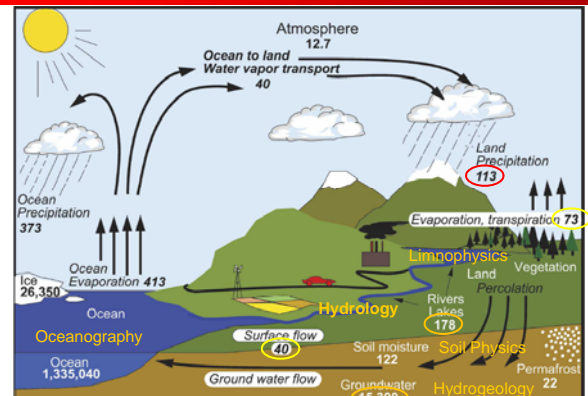
- By far largest freshwater reservoir
- partly difficult to access
- Usually clean (drinking water)
- slow renewal

Surface water:

- Rather limited Resource, esp. in arid regions
- Easily accessible
- Frequently polluted
- fast recycling

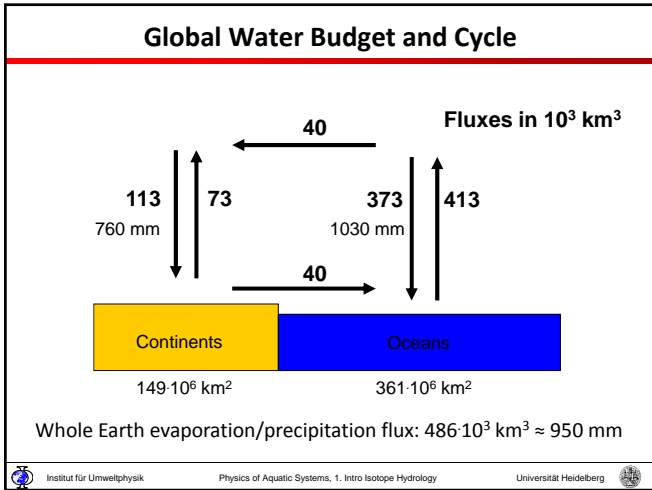
<http://www.unep.org/vitalwater/index.htm>

## 1.1 The Global Hydrological Cycle



Units: Thousand cubic km for storage, and thousand cubic km/yr for exchanges

Trenberth et al., 2007, J. Hydrometeorol. 8: 758 - 769



### Water Balance of the Continents

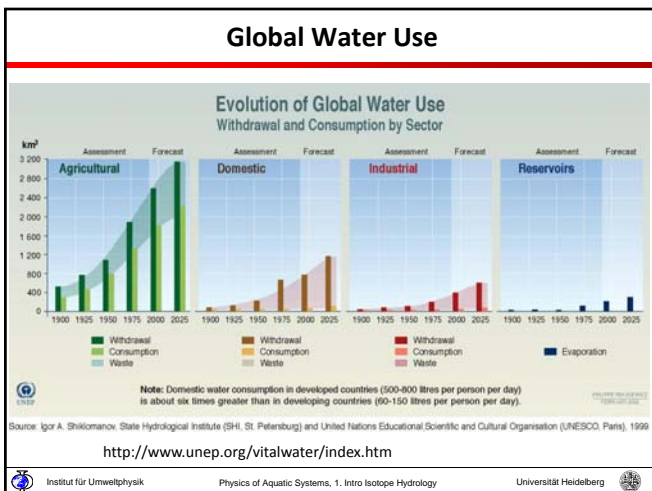
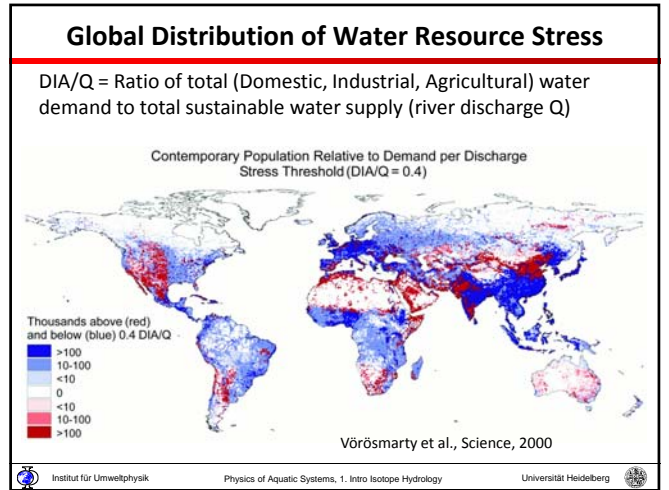
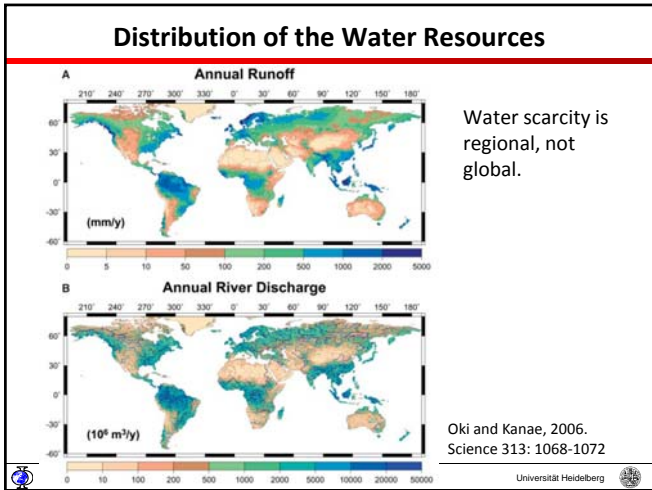
Component	Volume flux [km <sup>3</sup> /a]
<b>Input</b>	
Precipitation	113.000
<b>Output</b>	
Evapotranspiration	73.000
- Ecosystems	51.000
- Grassland	14.400
- Cropland	7.600
Runoff	40.000
- Withdrawals	3.800
<b>Sum Output</b>	<b>113.000</b>

"Blue" and "green" water

- green water: 30 % utilised
- blue water: 10 % utilised

renewable water resource: 40.000 km<sup>3</sup>/a  
realistically accessible: 13.000 km<sup>3</sup>/a  
present utilisation: ≈ 30 %

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### Irrigation

- produces 40 % of the world's food on 20% of the agricultural area
- accounts for 70% of the water withdrawals (3.000 of the available 13.000 km<sup>3</sup>/a)
- regionally overutilises surface and ground water

Hidden problem: non-sustainability

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## Unsustainable Water Use: Drying Lakes

Aral Sea

<http://www.unep.org/vitalwater/index.htm>

What has happened...



Lake Chad



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## Unsustainable Water Use: Drying Rivers

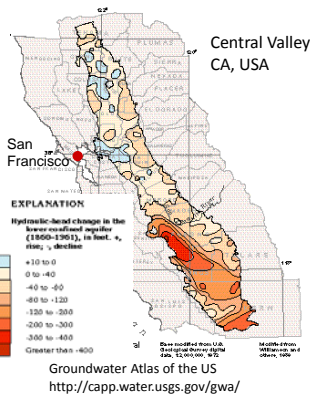


The Yellow River (Huang He) nowadays falls dry for about 4 months each year.



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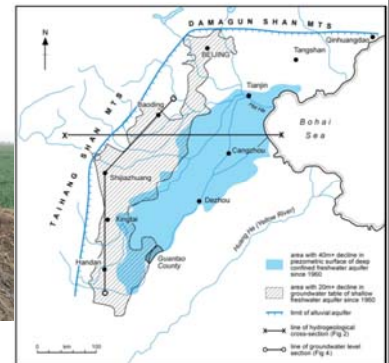
## Unsustainable Water Use: Falling Water Tables



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## Unsustainable Water Use: Falling Water Tables

North China Plain



Foster et al., 2004. Hydrogeol. J. 12: 81-93

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## 1.2 The Role of Water in the Environment

- Water permeates all spheres of the environment
  - important medium for transport (heat, substances)
- Basis of life
  - most abundant molecule in the biosphere
- Role of water in the climate system
  - Ocean: Heat storage and transport
  - Water vapour: greenhouse gas, clouds, latent heat
  - Snow, ice: high albedo

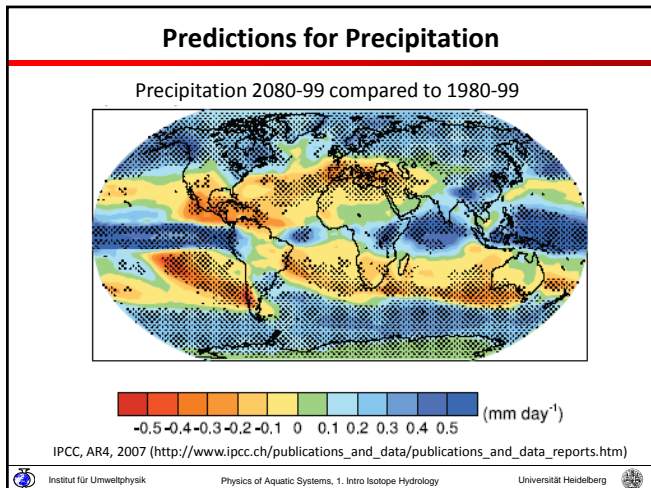
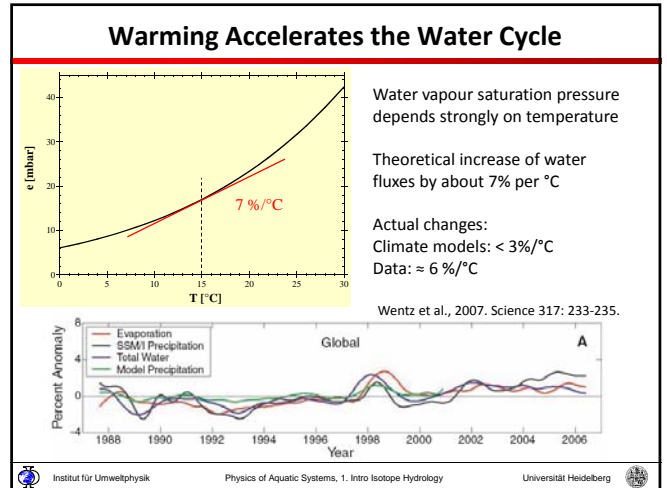
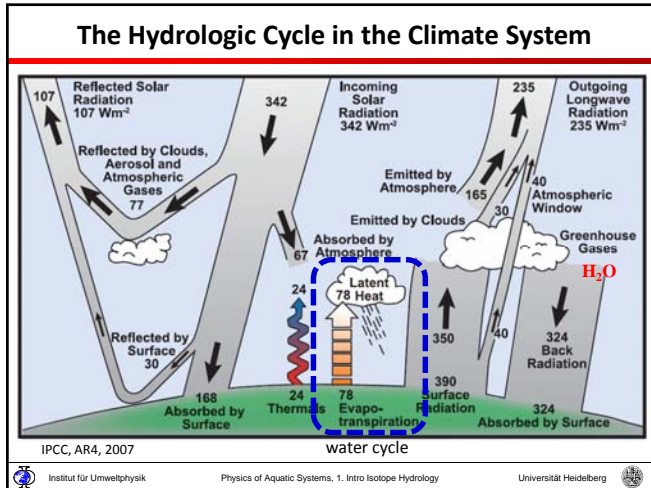
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## Role of the Ocean in the Climate System

### Facts on the ocean:

- Area:  $361 \cdot 10^6 \text{ km}^2$  (70 % of Earth's surface)
- Volume:  $1.365 \cdot 10^9 \text{ km}^3 \Rightarrow$  mean depth 3800 m
- Mass:  $1.4 \cdot 10^{21} \text{ kg}$  ( $\approx 280x m_{\text{atm}}$ )
- largest heat reservoir
- largest mobile  $\text{CO}_2$  reservoir
- large surface with low albedo

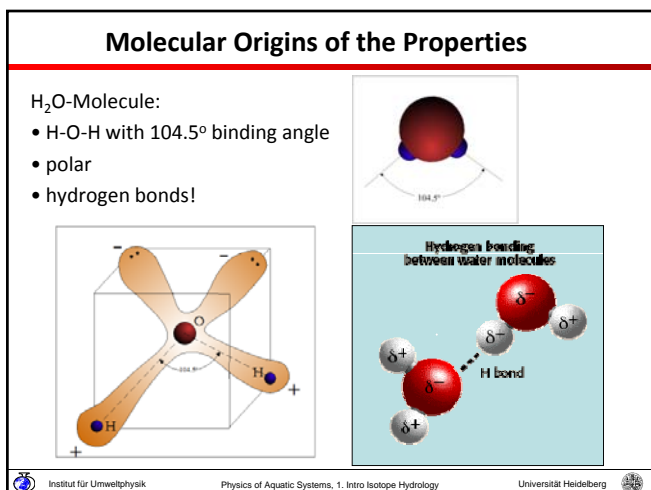
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### Physical Properties of Water

Property	Comparison	Importance, consequences
Specific heat 4180 J kg <sup>-1</sup> K <sup>-1</sup>	Highest of all solids and liquids except liquid NH <sub>3</sub>	Heat transport by water movement, heat buffering
Heat of fusion 3.34 · 10 <sup>5</sup> J kg <sup>-1</sup>	Highest except NH <sub>3</sub>	Thermostatic effect at freezing point
Heat of evaporation 2.25 · 10 <sup>6</sup> J kg <sup>-1</sup>	Highest of all substances	Heat and water transfer in the atmosphere
$\rho_{\max}$ at $T > T_{\text{freezing}}$ (~4 °C at 0%, 1 atm)	anomalous	Density stratification of lakes, facilitates freezing
$\rho_{\text{solid}} < \rho_{\text{liquid}}$	anomalous	Ice floats on water, freezing only at surface, weathering
Surface tension	Highest of all liquids	Drop formation, capillary forces, soil water retention, cell physiology
Dissolving power	Very high	Transport of dissolved substances
Dielectric constant	Highest of all liquids except H <sub>2</sub> O <sub>2</sub> and HCN	High dissociation of dissolved salts

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### 1.3 Specific and Latent Heat, Vapour Pressure

Tab. 1.3: Spezifische Wärme  $c_p$  und Umwandlungswärme von Wasser im Vergleich zu anderen Stoffen (siehe auch Tab. 1.4)

Eigenschaft	Wasser	Andere Substanzen
Spez. Wärme $c_p$ , 25°C [J·kg <sup>-1</sup> ·K <sup>-1</sup> ]	4.18 · 10 <sup>3</sup> a)	Al: 0.90 · 10 <sup>3</sup> Fe: 0.44 · 10 <sup>3</sup> H <sub>2</sub> -Gas: 14.3 · 10 <sup>3</sup> He: 5.18 · 10 <sup>3</sup>
	Eis, 0°C [J·kg <sup>-1</sup> ·K <sup>-1</sup> ]	2.11 · 10 <sup>3</sup>
Verdampfungswärme 25°C [J kg <sup>-1</sup> ]	2.44 · 10 <sup>6</sup>	CO <sub>2</sub> (0°C): 2.32 · 10 <sup>5</sup> NH <sub>3</sub> (0°C): 1.26 · 10 <sup>6</sup>
Schmelzwärme 0°C [J kg <sup>-1</sup> ]	3.34 · 10 <sup>5</sup>	

a) Zwischen 0 und 100°C variiert  $c_p$  nur um ungefähr 1% (s. Tab. 1.4).

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## Temperature Dependence of some Properties

Tab. 1.4: Einige physikalische Eigenschaften von Wasser bei Atmosphärendruck

Temp. T [°C]	Dampfdruck $e_w$ [mbar]	Spez. Wärme $c_p$ [J kg <sup>-1</sup> K <sup>-1</sup> ]	Verdampfungs-wärme [10 <sup>6</sup> J kg <sup>-1</sup> ]	Molek. Diff. für Wärme $D_T$ [10 <sup>-6</sup> m <sup>2</sup> s <sup>-1</sup> ]	Kinemat. Viskosität $\nu$ [10 <sup>-6</sup> m <sup>2</sup> s <sup>-1</sup> ]
0	6.1	4217.4	2.501	0.134	1.787
5	8.7		2.489		1.519
10	12.3	4191.9	2.477	0.138	1.307
15	17		2.465		1.14
20	23.3	4181.6	2.454	0.142	1.004
25	31.6		2.442		0.893
30	42.3	4178.2	2.43	0.146	0.801
35	56.2		2.415		0.724
40	73.8	4178.3	2.406	0.152	0.658
45	95.8		2.391		0.602
50	123	4180.4	2.382		0.553
60	199	4184.1	2.357	0.158	0.475
70	311	4189.3	2.333		0.413
80	473	4196.1	2.308	0.164	0.365
90	701	4204.8	2.283		0.326
100	1013	4215.7	2.257	0.166	0.294

## Saturation Vapour Pressure

Description of a phase transition

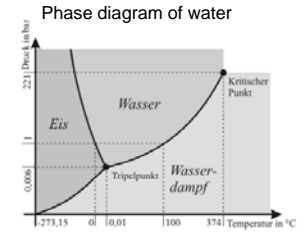
1 ↔ 2 by the

Clausius-Clapeyron equation:

$$\frac{dp}{dT} = \frac{L_{12}}{T(v_1 - v_2)}$$

L: Latent Heat

$v_i = 1/\rho_i$  = specific volumes



For vapour ↔ water:  $v_2 = v_w \ll v_v$  and  $v_v = \frac{RT}{p}$

Thus: 
$$\frac{dp}{dT} = \frac{Lp}{RT^2}$$

mit  $R_0 = R/M_w = 461.5 \text{ J kg}^{-1} \text{ K}^{-1}$

## Saturation Vapour Pressure

From Clausius-Clapeyron:

$$\frac{dp_s}{p_s} = \frac{L dT}{R T^2}$$

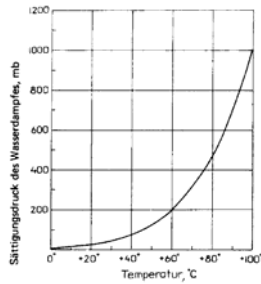
Integration gives

$$\ln \frac{p_s(T)}{p_s(T_0)} = -\frac{L}{R} \left( \frac{1}{T} - \frac{1}{T_0} \right)$$

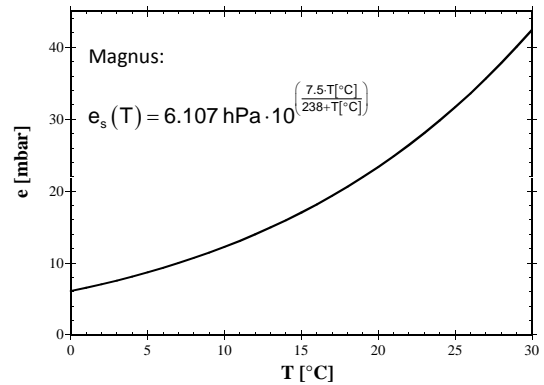
$$p_s(T) = p_0 \cdot \exp \left[ -\frac{L}{R} \left( \frac{1}{T} - \frac{1}{T_0} \right) \right]$$

e.g.:  $T_0 = 0^\circ\text{C}$ ,  $p_0 = 6.11 \text{ mbar}$ ,  $L = 2.5 \cdot 10^6 \text{ J kg}^{-1}$

In practice: Magnus equation 
$$p_s(T) = 6.107 \text{ hPa} \cdot 10^{\left( \frac{7.5T[^\circ\text{C}]}{238+T[^\circ\text{C}]} \right)}$$



## Saturation Vapour Pressure



## Summary

- Aquatic Physics looks at physical processes in aquatic systems
- The hydrological cycle is a central process in the environment
- The hydrosphere is an essential part of the climate system
- Humanity's use of water is about 30 % of the available resource
- In arid regions, over-exploitation occurs (drying lakes, rivers, etc.)
- Physical properties of water are quite extraordinary
- High specific and latent heat are important for the climate
- Vapour pressure strongly increases with temperature